

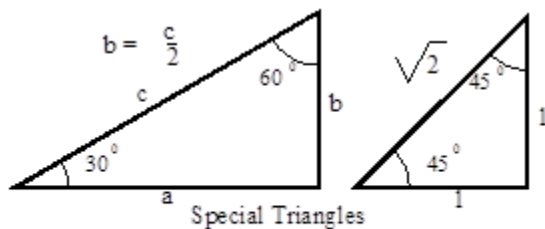
TMTH 205
FINAL EXAM FORMULA SHEET

CHAPTER 6: Geometry

NAME	FORMULA
Circle	Circumference = $2\pi r$ or πd
	Area = πr^2 or $\frac{\pi d^2}{4}$
Square	Perimeter = $4s$
	Area = s^2
Rectangle	Perimeter = $2(l + w)$
	Area = $l \cdot w$
Parallelogram	Perimeter = $2(a + b)$
	Area = $b \cdot h$
Rhombus	Perimeter = $4s$
	Area = $s \cdot h$
Trapezoid	Perimeter = $a + b + c + d$
	Area = $\frac{(a+b) \cdot h}{2}$
Triangle	Area = $\frac{b \cdot h}{2}$
Hero's Formula	Area = $\sqrt{s(s-a)(s-b)(s-c)}$ where $s = \frac{a+b+c}{2}$

NAME	FORMULA
Cube	Volume = a^3
	Surface Area = $6a^2$
Rectangular Parallelepiped	Volume = lwh
	Surface Area = $2(lw + hw + lh)$
Any cylinder or prism	Volume = (area of base) • (altitude)
Right cylinder or prism	Lateral Area = (perimeter of base) • (altitude) (not including bases)
Sphere	Volume = $\frac{4}{3}\pi r^3$
	Surface area = $4\pi r^2$

Any cone or pyramid	Volume = $\frac{h}{3} \cdot (\text{area of base})$ h = height of cone or pyramid
Right circular cone or regular pyramid	Lateral area = $\frac{s}{2} \cdot (\text{perimeter of base})$ s = length of slant side
Frustum	Volume = $\frac{h}{3} \cdot (A_1 + A_2 + \sqrt{A_1 A_2})$ h = height
Frustum	Lateral area = $\frac{s}{2} \cdot (\text{sum of base perimeters})$ $= \frac{s}{2} \cdot (P_1 + P_2)$: s = length of slant side



CHAPTER 18: Trigonometric Identities and Equations

$$\cot\theta = \frac{1}{\tan\theta} \quad \sec\theta = \frac{1}{\cos\theta} \quad \csc\theta = \frac{1}{\sin\theta} \quad \tan\theta = \frac{\sin\theta}{\cos\theta} \quad \cot\theta = \frac{\cos\theta}{\sin\theta}$$

$$\sin^2\theta + \cos^2\theta = 1$$

$$1 + \tan^2\theta = \sec^2\theta$$

$$1 + \cot^2\theta = \csc^2\theta$$

CHAPTER 20: Exponential and Logarithmic Functions

Growth

$$y = ae^{nt}$$

Decay

$$y = ae^{-nt}$$

Growth to an Upper Limit

$$y = a(1 - e^{-nt})$$

Compound Interest

$$y = a(1 + n)^t$$

$$y = a \left(1 + \frac{n}{m}\right)^{mt}$$

Doubling Time and Half-Life

$$t = \frac{\ln 2}{n}$$

$$\log_b N = a \quad b^a = N$$

$$\log \left(\frac{M}{N}\right) = \log M - \log N$$

$$\log (M \cdot N) = \log M + \log N$$

$$\log M^n = n \cdot \log M$$

CHAPTER 22: Analytic Geometry

Straight Line

Distance formula.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Equation of Straight line (General Form)

$$Ax + By + C = 0$$

Equation of Straight line (Slope-Intercept Form)

$$y = mx + b$$

Equation of Straight line (Point-slope Form)

$$m = \frac{y - y_1}{x - x_1}$$

$$\text{or } y - y_1 = m(x - x_1)$$

Equation of Straight line (Two-point form)

$$\frac{y - y_1}{x - x_1} = \frac{y_2 - y_1}{x_2 - x_1}$$

Intersection angle between two lines

$$\tan \phi = \frac{m_2 - m_1}{1 + m_1 m_2}$$

Circle

Standard Equation (Circle of Radius r)
Centre at (h, k)

$$(x - h)^2 + (y - k)^2 = r^2$$

Parabola

Standard Equation (Vertex at origin)
Axis Horizontal

$$y^2 = 4px$$

Standard Equation (Vertex at origin)
Axis Vertical

$$x^2 = 4py$$

Focal Width

$$L = |4p|$$

Ellipse

Standard Equation (Centre at origin)
Major axis vertical

$$\frac{y^2}{a^2} + \frac{x^2}{b^2} = 1$$

Standard Equation (Centre at origin)
Major axis horizontal

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

Distance from centre to focus.

$$c = \sqrt{a^2 - b^2}$$

Focal width (where a is semi-major axis)

$$L = \frac{2b^2}{a}$$

Hyperbola

Standard equation (Trans. horizontal)

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad \text{slopes of asymptote} = \pm \frac{b}{a}$$

Standard equation (Trans. vertical)

$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1 \quad \text{slopes of asymptote} = \pm \frac{a}{b}$$

Distance from centre to focus

$$c = \sqrt{a^2 + b^2}$$

Focal Width

$$L = \frac{2b^2}{a}$$